Techniques and Applications for Strain Measurements of Skeletal Muscle

5

5.1 Introduction

Determination of the constitutive properties and failure tolerances has been a principal activity of solid biomechanics for many years. Unlike engineering materials, however, the tissues and cellular structures of the body demonstrate uniquely challenging material behavior making the measurement of constitutive and failure properties difficult. In the face of these challenges a large experimental effort has occurred which has resulted in an increasingly accurate determination of the tensorial quantities upon which tissue properties and tolerances are dependent. In particular, the ability to measure strain in compliant, non-linear, hydrated, biologic tissues has become particularly refined. Yet, the selection of the appropriate formulation of strain, and the techniques used to measure strain vary widely. In this chapter, we present an overview of these techniques with particular reference to the measurement of strain in muscle.

5.2 Strain Theory

A wide variety of mathematical and experimental representations have been developed to quantify the components of strain within a deformable body. Most experimental methods quantify some component of motion and deformation and compute the strain components of interest based on a given strain formulation. In that regard, we present a review of deformation theory as given by Lai et al. As a central underlying theme, strain measurement allows a quantification of the continuous, internal deformations of a material which are not the result of rigid body motions. Consider the point \( P_0 \) in the material located a distance \( X \) from the origin (Fig. 5.1). As a result of a change in position, \( u(x) \), the point \( P_0 \) is translated to a new position \( P \) at some subsequent time. The location of the point \( P \) is described by the vector \( x \) where \( x = X + u(X) \). In that regard, \( u(u, v, w) \) represents the motion of the point \( P_0 \) over time, where \( u, v, \) and \( w \) represent the components of motion in three orthogonal directions and are functions of position on the body, \((x, y, z)\). To describe the state of strain at the point \( P_0 \) in the material we will
examine changes in the length between $P_0$ and a closely neighboring point $Q_0$. The location of $Q_0$ is given by $X + dX$. At the same subsequent time, $Q_0$ translates to the new location $Q$. The new location of $Q$ is given by $x + dx$, and its translation is described by $u(X + dX)$. These quantities are related vectorially by

$$x + dx = X + dX + u(X + dX)$$

Recalling that $x = X + u(X)$, this equation can be rewritten as

$$dx = dX + u(X + dX) - u(X) = dX + (\nabla u)dX$$

where $\nabla u$ is the displacement gradient. For Cartesian coordinates $\nabla u$ is given by

$$\nabla u = \begin{bmatrix} \frac{\partial u_i}{\partial X_1} & \frac{\partial u_i}{\partial X_2} & \frac{\partial u_i}{\partial X_3} \\ \frac{\partial u_2}{\partial X_1} & \frac{\partial u_2}{\partial X_2} & \frac{\partial u_2}{\partial X_3} \\ \frac{\partial u_3}{\partial X_1} & \frac{\partial u_3}{\partial X_2} & \frac{\partial u_3}{\partial X_3} \end{bmatrix}$$

Further, we can define the deformation gradient, $F$, as

$$dx = F dX$$

Substituting this for $dx$ in Eq. 5.2 and solving for $F$ results in

$$F = I + \nabla u$$

where $I$ is the identify matrix. To quantify the deformation in a small neighborhood around $P_0$ we compare the length of the vector $dX$, denoted by the scalar quantity $dS$, to the length of the vector $dx$ denoted $ds$, resulting in the following equation:

$$(ds)^2 = dx \cdot dx = F dX \cdot F dX = dX \cdot F^TF dX$$
Consider the special case of rigid body motion in which \( F \) is an orthogonal matrix comprised of orthonormal vectors such that \( F^T F = I \). Upon substitution into Eq. 5.6 results in \( ds^2 = dX \cdot dX = dS^2 \). Subject to this condition, the length is unchanged and the deformation gradient represents a rigid body rotation of the two points from their initial to their final positions. To define a strain tensor that is independent of rigid body motion, it is necessary to separate out the orthogonal portion of \( F \). Using the polar decomposition theorem, we can write

\[
F = RU = VR
\]  

(5.7)

where \( U \) and \( V \) are positive definite symmetric tensors and \( R \) is an orthogonal tensor representing the rigid body motion. It can be shown that this is a unique decomposition in which \( U \) and \( V \) are known as the right and left stretch tensors, respectively. Using Eq. 5.76, it follows that

\[
F^T F = (R U)^T (R U) = U^T R^T R U
\]  

(5.8)

However, because \( R \) is orthogonal, \( R^T R = I \), and Eq. 5.8 simplifies to

\[
F^T F = U^T U
\]  

(5.9)

Using this formulation, several strain tensors can be defined. The right Cauchy-Green deformation tensor, \( C \), is defined as

\[
C = F^T F
\]  

(5.10)

The left Cauchy-Green deformation tensor, \( B \), is defined as

\[
B = FF^T
\]  

(5.11)

The Lagrangian finite strain tensor, \( E \), is defined as

\[
E = 1/2(C - I)
\]  

(5.12)

Rewriting \( E \) in terms of the vector \( u \) results in the following expression:

\[
E = 1/2(\nabla u + (\nabla u)^T) + 1/2(\nabla u)^T(\nabla u)
\]  

(5.13)

Expressed in tensorial notation, this gives rise to the commonly used expression

\[
E_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial X_j} + \frac{\partial u_j}{\partial X_i} \right) + \frac{1}{2} \frac{\partial u_m}{\partial X_i} \frac{\partial u_m}{\partial X_j}
\]  

(5.14)

where \( m \) is a summed index. Each of these quantities results in a second order tensorial definition of strain tensor. Each component of the strain tensor can be determined if the full three-dimensional displacement field, \( u(u, v, w) \), is known. Fortunately, in many situations, it may not be necessary to use such a generalized representation of strain. However, it should also be recognized that, even in problems in which only the uniaxial normal strain is to be determined, the three-dimensional displacement field may require characterization. Examination of the Lagrangian representation of strain for the characterization of the axial strain, \( E_{xx}(x, t) \), illustrates this phenomenon:
In this situation, gradients of the all three deformation terms are required to characterize a single normal strain. However, if the spatial gradients of the displacements are small, the so-called small strain problem, the higher order terms may be neglected and the commonly used one-dimensional small strain formulation results. This formulation is only valid if the higher order terms remain small with respect to the first order gradient terms. For example, a displacement gradient of $\frac{\partial u}{\partial x} = 0.15$ results in a Lagrangian strain of 0.161. Using small strain theory, an underestimation of strain of 0.011 results, representing an error in strain measurement of 7%.

Another commonly used convention is the stretch ratio. The stretch ratio, $\lambda$, is defined as

$$\lambda = \frac{\Delta L}{L}$$

(5.17)

The stretch ratio is not a tensorial component of strain. However, the stretch ratio is a convenient way to report finite uniaxial deformations with a more obvious direct physical significance. Further, if measured in the appropriate directions, three stretch ratios can completely define other tensorial definitions of strain, like the left Cauchy-Green strain tensor. This approach has been used together with the assumption of incompressibility to model rubber, mesentery, muscle, and brain.18,21,52,76,84,107,110

Ultimately, the choice of the method used to define strain will depend on the type of problem, the constitutive formulations, and the available experimental data. Regardless of the strain formulation, however, careful definition of the strain components measured in a given study is a requirement for the generation of meaningful data.

### 5.3 Experimental Considerations

In making mechanical measurements of soft tissue, a need to reproduce the *in vivo* environment is required if meaningful results are to be obtained.14,30,44,80,116 For example, the constitutive behavior of many biological tissues has been shown to be both temperature and hydration sensitive.30,80 Mechanical stabilization, or preconditioning, a process in which the tissue is cycled repeatedly at the onset of a test battery, has also been shown to influence soft tissue behavior, and is necessary for generation of repeatable constitutive data.36,67,116 Soft biologic tissues are also sensitive to the loading rate and duration which can vary from a few milliseconds during impact injury to seconds and hours in activities of daily living.47,66,79 Several tissues, most notably skeletal muscles, undergo very large strains during physiologic loading. Zajac reports that the tibialis anterior of the rabbit experiences a change in length between 15 and 20% during hopping.120 Changes in length between 10 and 50% have been reported in the lower extremity of the cat during gait.34 Using a computational model, Merrill et al. suggested that the muscles of the human cervical spine elongate as much as 40%.71 Additionally, as experimental test specimens are often removed from their anatomic origins and insertions, specific attention to the effects of the *in vitro* conditions is required. That is, the loads applied by the experimental apparatus must mimic those applied in the *in vivo* environment, and the strain measurement technique must account for the effects of the nonphysiologic end conditions on the measured deformation. A novel solution to this problem, which allows for the appropriate selection of end loads, and provides estimates of *in vivo* loads is the measurement of strain *in vivo*. Hawkins et al. measured strains of rabbit medial collateral ligament *in vivo* where force...
measurements are impossible because of the redundant construction of the knee ligaments. The ligament was then tested \textit{in vitro} and the loads required to impose similar strains were determined and used as estimates of the \textit{in vivo} loads.\textsuperscript{44}

Accurate measurement of soft tissue strain is made more complex by the material heterogeneity of biologic structures in which the soft tissues of the body often show strong regional variations. In muscle, this includes the anatomically distinct regions of the tendons, aponeuroses, and the muscle fibers. For example, testing of whole muscle tendon units reported in Lieber et al. resulted in average normal strains in the mid-tendon, tendon-bone interface, and aponeurosis of 2, 3.4, and 8\%, respectively.\textsuperscript{60} Variations in the time-dependent responses of the components of muscle add a rate sensitivity to the regional variations in strain. According to Best et al., differences in mid-muscle belly Lagrangian strains of 30\% are reported as the rate of elongation of the tendon increased from 40 to 100 cm/sec.\textsuperscript{8} Strain fields also vary from regional variations in material properties within a given muscle. As a result, even small test specimens can have wide variations in their constitutive properties resulting from an inhomogeneous strain field, despite having uniform test specimen geometry. Mechanical measurement in muscle is also made more complex by the variations in area, and therefore stress, along the length of the test specimen, as occurs commonly during whole skeletal testing.\textsuperscript{77}

Measurement of skeletal muscle strain is made uniquely complex by the tissue's need to have proper reproduction of its \textit{in vivo} environment. Specifically, the mechanical properties and hence deformations of skeletal muscle are dependent upon both a passive extracellular matrix, and a dynamic, metabolically dependent, intracellular protein interaction. In contrast, many passive biological tissues such as bone, ligament, tendon, and skin derive their mechanical properties exclusively from extracellular matrix interactions. The intracellular responses depend strongly on the normal function of the cell, in addition to the correct electrical excitation of the membrane. For these reasons, both nutrients and electrical potentials must be supplied to the muscle during testing through either an intact neurovascular supply or through a nutrient-rich bath using specimens of sufficiently small size to allow for the delivery of nutrients by diffusion alone. Gaining access to the tissue for deformation measurement is made increasingly difficult by these additional experimental design considerations.

Considering only the passive responses, skeletal muscle still represents a complex experimental challenge. Several investigators have shown that the passive mechanical properties of skeletal muscle are a result of mechanical load carried by both intracellular and extracellular proteins.\textsuperscript{65} As a result of post-mortem intracellular proteolysis,\textsuperscript{102} the intracellular load carrying potential is lost, and the ability to study cadaveric muscle is profoundly limited. Indeed, skeletal muscle experiences large changes in its mechanical properties postmortem despite using currently accepted methods for storage of bone, ligament, tendon, cartilage, and skin.\textsuperscript{26,27,35,58} These changes include a decrease in stiffness of 47\%,\textsuperscript{35} and a decrease in strain at failure of 44\%.\textsuperscript{58} Fitzgerald\textsuperscript{26,27} reported the onset of changes in skeletal muscle mechanical properties within the first 6 hours of death. Our own laboratory studies characterizing the mechanical properties of skeletal muscle in the rabbit tibialis anterior support these observations (Fig. 5.2). The onset of rigor can be seen as early as 6 hours postmortem. By 8 hours postmortem, stiffness increased 600\% over the live passive muscle stiffness. Following this initial stiffness increase, which peaks at 12 hours postmortem, a gradual decrease in stiffness occurs over postmortem hours 12 to 62.5 resulting in a final muscle stiffness which is 28\% less than the live passive muscle stiffness.

Despite using methods that have been developed for storage of bone, ligament, and tendon, there are no standardized methods to store whole muscles or cadavers through the postmortem period that maintain the integrity of the microstructure and associated mechanical properties under the action of postmortem enzyme activity. For this reason, investigators have developed methods to store and test single muscle fibers.\textsuperscript{104,105} The fibers are mechanically\textsuperscript{78,86,87} or more often, chemically skinned\textsuperscript{23} disrupting the sarcolemma while leaving the myofibrillar structure intact. The fibers are then placed in a storage solution where the enzyme activity is modulated, resulting in the preservation of the intracellular protein structure. The fibers' mechanical properties are thereby stabilized, and the tissue can be frozen for months and tested without alterations in the mechanical properties. Further, the disruption in cell membrane
integrity allows for more direct access to the interior of the cell, allowing cell activation, relaxation, and rigor by altering the fluid bath which surrounds the cell.\textsuperscript{75} Maintaining tissue hydration for \textit{in vivo} experimentation is required during testing to avoid changes in mechanical properties due to drying.\textsuperscript{30} This has been accomplished experimentally using repeated applications of normal saline,\textsuperscript{8} continuous normal saline drip,\textsuperscript{43,\textsuperscript{58}} application of a thin film of paraffin oil,\textsuperscript{108} immersion within a fluid bath,\textsuperscript{60} covering with moist gauze,\textsuperscript{10} or enclosing within a 100% humid environment. Within muscle, an intact neurovascular supply aids in tissue hydration; however, care should be taken to keep the surface moist. Results of hydration methods for ligament and tendon are conflicting. Woo et al. report dehydration of tendon to cause increased stiffness and increased failure stress.\textsuperscript{116} Consistent with this finding is a study by Haut and Little where immersed ligaments were found to have a decreased modulus when compared to ligaments only slightly moistened.\textsuperscript{40} In contrast, a later study by Haut and Powlinson\textsuperscript{42} reported increases of 43 and 61% of tensile strength and stiffness for immersed specimens compared to specimens moistened by a drip method of the same solution. A source for some of these inconsistencies may be the effect of strain rate. In a study by Haut and Haut, changes in water content of tendon had no effect on mechanical properties at a strain rate of 0.5%/s, but at a strain rate of 50%/s, tissues with higher water content were 20% stiffer.\textsuperscript{41} In an effort to better understand the \textit{in vivo} conditions and the effects of different immersion solutions, Chimich et al. measured water content of ligament immediately after sacrifice and compared it to ligament water content after soaking in phosphate buffered saline (PBS) and 2, 10, and 25% sucrose solutions.\textsuperscript{14}

Water content immediately after sacrifice was found to be 64% ± 6% while contents of PBS and the 2, 10, and 15% solutions were found to be 74, 69, 60, and 51%, respectively. Relaxation tests were performed upon the four immersed tissues and higher water contents were associated with a greater degree of load relaxation. However, tests on the properties of the fresh ligament were not reported. The need to reproduce the \textit{in vivo} hydration within articular cartilage is also documented. Elmore et al. demonstrated the \textit{in vivo} recoverability of articular cartilage if immersed in a balanced salt solution.\textsuperscript{24} In

\textbf{FIGURE 5.2} Structural responses of live passive skeletal muscle, and the changes in passive properties that occur over time. The onset of rigor can be seen as early as 6 hours postmortem. By 8 hours postmortem, stiffness has increased 600% over the live passive muscle stiffness. Following this initial increase, which peaks at 12 hours postmortem, a gradual decrease in stiffness occurs over postmortem hours 12 to 61.5 resulting in a final muscle stiffness which is 28% less than the live passive muscle stiffness.
contrast to tendon and ligament, the recoverability of articular cartilage was closely linked to the tonicity of the solution. Previous experimenters testing in air had reported residual deformations after the load had been removed and had termed this experimental artifact the “imperfect” elasticity of articular cartilage. Appropriate selection of the hydration in the extra-specimen testing environment and careful consideration of the importance and physiologic relevance of tissue swelling and ion movement are therefore equally important requisites to the measurement of meaningful in vitro strains.

Temperature has also been shown to significantly affect the properties of skeletal muscle. While the properties of collagen have been shown to be relatively insensitive to changes in temperature ranging from 0 to 37°C, the properties of muscle have been shown to change over a range in temperature from 25 to 40°C. Specifically, stiffness decreased 11 to 15% while deformation to failure was unchanged. To standardize conditions of testing environment, a majority of investigators have chosen to use environmental chambers to control both humidity and temperature.

The ability to determine the properties of soft tissue is limited because the loading conditions along the tissue boundary are often unknown or difficult to recreate. Yet when the tissue is excised and evaluated in vitro, recreation of these in vivo loads and boundary conditions is requisite to the generation of meaningful constitutive data. Indeed, several investigations have shown that measured constitutive and tolerance data depend upon the methods by which the load is applied. To realize appropriate loading conditions in vitro, investigators have developed a wide variety of gripping devices and methods Directly gripping the specimen is among the most common methods used in biomechanics. Most grips compress the tissue in a clamp with the hope of distributing the load such that the specimen neither slips in the clamp nor suffers excessive damage in the clamp. Clamp designs are numerous and include direct clamping by smooth or patterned metal grips, or sinusoidal shaped grips. Capstan grips, in which the tissue is wrapped around a cylindrical shaft and clamped, are also employed. These have the advantage of decreasing the load on the tissue at the clamp at the expense of allowing slip in the specimen around the capstan. However, assuming a constant coefficient of friction between capstan and grip can provide estimates of the tissues spoolout during loading. Other approaches include the use of cyanoacrylate adhesive, embedding the tissue in polymethacrylate, and freezing the tissue directly to the clamps. To minimize gripping effects, investigators have tested bone-tissue-bone specimens to evaluate the mechanical properties of ligament, tendon, and muscle. Gripping of bone results in more physiologic load distribution in the soft tissue as the tissue’s anatomic origin and insertion are preserved. Further, the bone is more easily gripped without risk for slip or mechanical failure at the grip site.

Variations in strain distribution near the clamp are also thought to influence results. Saint-Venant's principle states that end conditions whose resultant force and couple are zero will not influence the state of stress and strain at distances that are large compared to the dimension over which the load is applied. Experimentally, this implies that any state of stress with an equivalent resultant force and couple at the grips will not alter the expected state of stress or strain remote from the clamps. Thus, for well-behaved test specimens, the midsubstance stress and strain distribution will not be affected by the end conditions and will approach the theoretical solution remote from the point of application of the load as though an ideal load distribution had been applied. Experimentally, this requires long, slender specimens and a path for load redistribution within the specimen that cannot always be realized with biomechanical specimens. The significance of gripping effects was noted by Butler et al. Midsubstance tendon strains were found to be 25 to 30% of strains near the grips or at the bone-tendon junction. Haut reported changes in maximum failure strain of small collagen test specimens as a function of specimen length. Surprisingly, Haut reported maximum strains at failure of 8.1% ± 0.3%, 8.5% ± 0.6%, and 17.6% ± 1.2% for specimen gauge lengths of 100, 50, and 10 mm, respectively. Interestingly, the failure load was insensitive to specimen length.

Increasing interest in the biomechanical behavior of cells has resulted in development of methods to grip and measure strain on the surface of cells. Barbee et al. measured strains on the ventral cell surface of cultured vascular smooth muscle cells. Cell deformations were imposed by deforming the compliant polyurethane substrate to which the dorsal surface of the cell was adherent. As in testing of larger structures, this adhesion gripping technique has been criticized. Concerns over failure of the cell to adhere

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to the membrane or cell injury as a result of membrane deformation are commonly raised. However, Anderson et al. provide data on the strains of cultured lung, muscle, and bone cells which refute these assertions. They report a close agreement between cell strain and estimated membrane strain. They also found no changes in membrane permeability, a sign of cell damage with strain, as measured by both fluorescent and trypan blue straining techniques.

Realization of optimal clamping technique without either slip or inappropriate failure with the clamps remains a challenge in biomechanical testing. With regard to strain measurement, the use of more complex experimental measures of strain than simple grip-to-grip excursions can often decrease the demands placed on clamp design and performance. That is, by measurement of full-field strain, the effects of the end conditions on deformation can be accounted for and less constraining clamps or enlarged grip surfaces can be employed. This is particularly relevant in failure testing in which the issue must fail at sites remote from the clamp in order to be considered meaningful. Thus, the ease with which the specimen can be coupled to the test apparatus often serves to define the type of strain measurement technique which should be used.

Most measures of strain require, or are based on, a definition of the undeformed geometry or a reference length in uniaxial problems. While often easily and uniquely defined for engineering materials as the specimen's zero load state, such definitions are less apparent in biologic tissues. Soft biologic tissues are typically compliant, nonlinear, strain-stiffening materials which show a large low-load region at small strains. As a result, small differences in the tare load (preload) used to mount the specimen can result in profoundly different initial positions. Further, creep effects under constant load can result in shifts in a load-based initial reference length over the duration of testing. In other words, subject to a load, the reference length changes with time. In order to manage this problem, authors have suggested fitting the load-elongation data and extrapolating to a no-load length. Other techniques to help define a reliable reference length in muscle include using a gross anatomic position, a microanatomic position, or a physiologic position. Garrett et al. established the initial length of the rabbit tibialis anterior based on an anatomical position by measuring the muscle length when the knee and ankle were both flexed to a joint angle of 90°. In situ sarcomere length may also be used. The force-length relationship of stimulated skeletal muscle has also been used to define a physiologic initial position. Specifically, by electrically twitching a muscle at various lengths the initial position of the muscle can be defined as the length at which maximum twitch force is measured. In the same context, the minimum length and maximum length at which no force is generated in response to an electrical stimulus may also be used as a reference length. Relationships between sarcomere length, whole muscle length, and twitch properties may allow for comparisons of data generated using these different gauge lengths. Measurements of the reference state of cardiac muscle are often based on gating the position-time histories with the cardiac cycle or cardiac electrical stimulation. In either case, clear definition of a reproducible reference length is requisite in strain measurement.

### 5.4 Displacement Measurement

Selection of the displacement measurement strategy is predicated on several factors including the physical constraints imposed as a result of the need to create a physiologically appropriate testing environment and the formulation of strain to be reported. Design considerations include the degree of intrusion imposed by the measurement system on the tissue, the required measurement accuracy, the frequency content of the experimental data, and the frequency response of the measurement system. Also of importance are the need to measure surface or internal deformations and the need for real-time displacements or post-test data analysis to determine displacements. Other considerations include the cost of the system, the ease of use, the number of dimensions to be measured, and the need for average or full-field measures of displacement. In light of the diversity of design considerations, it is of little surprise that the techniques employed vary widely.

Like many other tissues in the body, skeletal muscle exhibits a hierarchal structural organization. Among the most significant functional building blocks of whole skeletal muscle is the sarcomere. Indeed,
whole muscle structural properties may be derived directly from the organization of sarcomeres. Specifically, force production is proportional to the numbers of sarcomeres arranged in parallel, while the maximum tendon velocity is proportional to the number of sarcomeres in series. Sarcomere lengths range from 1.5 to 4.0 µm and both stimulated and passive muscle responses have been shown to be functions of the sarcomere length. In that regard, measurement of constitutive properties as a function of sarcomere length as opposed to strain is a common practice. The two most common methods to measure sarcomere length are laser diffraction and microscopy.

Microscopy affords direct observation of the tissue and has been useful in determining complex microstructural interactions. However, the size and proximity of the optics often preclude sarcomere measurements during mechanical testing except for single muscle fiber preparations. In an effort to automate sarcomere length measurements, captured microscopic images of muscle cell striations by video. Sarcomere lengths over a population of cardiac cells were determined by using a Fourier transform in which the spatial frequency of the spatially periodic sarcomeres was determined. The laser diffraction technique also makes use of the periodic structures of the sarcomeres in the muscle fiber. Acting as a diffraction grating, a monochromatic light passing through the fibers produces a diffraction pattern in which the distance between the first set of parallel lines is proportional to the sarcomere length. The laser affords the advantage of being able to measure average sarcomere lengths through a thicker sample than compared to microscopy. As a result, dissection times are substantially reduced using laser techniques. Laser techniques have the additional advantage of adaptability for use in measuring in situ sarcomere length. Fleeter et al. used laser techniques to measure sarcomere length of human forearm muscles in situ for use in tendon transfer surgeries to determine optimal muscle length before attachment of the tendon. Trestic and Lieber were also able to make in situ sarcomere length measurements. Using the frog gastrocnemius muscle, in which the central tendon typically precludes whole muscle diffraction measurements, these authors showed that diffraction measurements on partially dissected bundles containing approximately 100 fibers compared favorably with those of the intact muscle. Lieber et al. were also able to automate the laser diffraction method to measure sarcomere length in single muscle fiber tests. They report a frequency response of 3.8 kHz and a measurement accuracy of 0.043 µm. Thus, in single fiber measurement, laser diffraction techniques provide higher frequency response but somewhat lower spatial resolution than microscopy techniques.

Analogous techniques have also been used on tendons. Sasaki and Odajima measured microstructural deformation in tendons using X-ray diffraction. Using a wide-angle X-ray diffraction technique, reflections were produced corresponding to distances between neighboring amino acids along the helix of the collagen molecule. Using small-angle X-ray diffraction, the fibrillar organization of whole collagen molecules was measured. Interestingly, these authors have also used microscopy techniques to measure tendon strains, and have reported an accuracy on the order of ±0.1%. These measurements have led to the development of structural models based on true microstructural interactions of collagenous tissues.

In contrast to microstructural measurements, tissue deformation can be measured on a macroscopic scale using transducers which directly measure displacement. Grip-to-grip measures of displacement are among the easiest and most commonly used. This method typically measures actuator motion for a specimen with a grip mounted to the actuator, and another grip mounted to a fixed platen. The actuator is usually instrumented with a linearly variable differential transformer (LVDT) which serves as a feedback signal for the control algorithm. This signal is split, acquired digitally, and used as a measure of tissue displacement. In that regard, the tissue motion can be measured without the use of additional instrumentation. While a wide variety of transducers can be used to measure displacement, the LVDT is the most common, owing to its excellent frequency response, variable sensitivity, stability, and fatigue-resistant design. The devices are AC transformers which detect changes in the magnetic field as a magnetically permeable core is moved within the field. As a result, the moving core is not in direct contact with the housing, and fatigue effects are minimized. The accuracy of the displacement measurement of a typical LVDT is between 0.5 and 0.25% of full scale stroke. Full scale stroke ranges from as little as 0.1 to 650 mm. Data can be acquired at frequencies up to 10% of the excitation frequency and
excitation frequency varies from 60 Hz to 25 kHz, although higher frequencies are attainable. Linear potentiometers can also measure displacement; they are considerably less expensive, approximately 10% of the cost of an LVDT. However, they lack the sensitivity and flexibility of an LVDT and are prone to fatigue as they operate through a contact mechanism. For strictly static measurements, dial gauges have also been used but viscoelastic effects can confound static measurement techniques. Dial gauges typically provide measurement accuracies on the order of ±0.0125 mm.

While often used because of the ease of testing a whole muscle tendon unit, grip-to-grip measures are not without limitations. The method is predicated on the use of a stiff load frame, such that test frame deformation does not corrupt the displacement measurement. For example, Lieber et al. reported a system compliance of 1.3 µm/g when measuring displacements of 13 mm under peak loads of 2000 g. Another limitation with this method is the heterogeneity of the tissue between the grips. In testing whole muscles with long tendons, the deformation of the tendon and aponeurosis can be significant, despite subjection to smaller strains than the muscle. Trestik and Lieber report the results of an experiment in which the gastrocnemius-Achilles tendon complex was stretched. Strain within the complex varied from 2% in the tendon up to 8% in the aponeurosis when muscle strains of 15% were observed. Clearly, an assumption that the measured displacement could be assigned directly to the muscle would result in substantive errors in assumed muscle strain.

Of greatest concern with this technique is the possibility of slip of the specimen within the grips, particularly during failure testing. In general, larger measurements of deformation, and therefore strain, are recorded when using bone-to-bone to grip-to-grip methods rather than when displacements are measured within the tissue midsubstance. Studies by Haut, Zernicke et al. and Butler et al. found significant differences in the calculated modulus, failure strain, and failure strain energy density when using grip-to-grip methods as compared to regional measures of displacement. Even when slip is minimized through the use of good gripping technique, the effects of gripping on local tissue deformation can be significant. Zernicke et al. reported strains as great as 60% close to the grips while measured strains remote from the grips were less than 15%. After testing gracilis, semitendinosus, fascia lata, and patellar tendon-bone units they reported that grip-to-grip measurements of strain were 3.2 times larger than averaged regional values through the midsection of the specimen.

The most common solution to the errors associated with grip-to-grip measurement in engineering has been the use of dumbbell-shaped specimens with a midsubstance over which displacements are measured. Clip gauges and extensometers have been commonly used to measure midsubstance displacements, though they require more robust specimens than are often found in biomechanics. Clip gauges have been developed using spring steel and other materials. They make use of a strain gauge mounted on an arched flexible strip formed to the desired gauge dimensions. Clips at the ends of the strip are coupled to the tissue using glue, sutures, or clamps. Design and selection of these devices ultimately become a trade-off between intrusion (the loads imposed on the system by the measuring device which can alter the deformation and damage the tissue) and displacement sensitivity and frequency response. Potentiometers and LVDTs can also be used in similar applications, although the need to maintain the coaxial orientation of the core and housing can prove difficult.

Because of its versatility in design and very low cost, the foil strain gauge has also enjoyed popularity as a direct contact measurement of tissue strain, although its use is limited to higher modulus materials like bone. Strain gauge concepts have been adapted for use with more compliant soft tissues like tendon and ligament. For example, liquid metal strain gauges make use of mercury-filled silastic tubes that are sutured directly to the surface of the tissue. Described in detail by Brown et al. and Meghan et al., these devices operate through the same mechanism as the foil gauge. As the tube's length is changed, the cross section is altered and the resistance changes. Meghan et al. used this gauge to measure anterior cruciate ligament strain. Van Weeren et al. measured the in vivo strains of the peroneous tertius tendon of a horse. Brown et al. measured the dynamic performance of these gauges and their applicability to measurements of soft tissue strain. The gauges were found to be linear up to 40% change in length. In addition, gauges exhibited frequency independent response up to 50 Hz for a cyclic 20% change in length. Stiffness of the gauge was found to be 0.024 N/mm, which is approximately 4% that of tendon. However,
the shelf life of the gauges is limited to about 3 months due to the oxidation of the mercury through the silastic tubing.

Arms et al. used a Hall effect sensor to estimate strains in the medial collateral ligament. A semiconductor device measured the proximity of a permanent magnet attached to the tissue. Cholewicki et al. also employed a Hall effect device to measure motion between the facet surfaces of the intervertebral joint. The device's range of motion was 4 to 12 mm with a reported accuracy of 0.025 mm. Frequency response of the sensor was reported to be 20 kHz; however, mass effects associated with the guide track, sensor, and magnet will likely limit frequency performance to a value considerably below the sensor response. Additionally, the calibration of this device was nonlinear, making its use somewhat more difficult. While the cost of a Hall effect sensor is typically less than a dollar, the mounts must be designed and assembled by the investigator. Commercially available sensors are available; the cost is approximately $900.

Villarel et al. and Omens et al. describe the use of three piezoelectric crystals to determine planar displacements of the left ventricle of the heart. Each crystal both receives and transmits signals to the other two crystals resulting in measures of length based on assumptions regarding transmission velocity in the media. Frequency response of the system was 375 Hz. Accuracy of the system was not calculated, but results were similar to those derived from using biplane coneradiography.82,111

George and Bogen report the design, construction, and use of a novel biaxial fiberoptic strain gauge system.32 The system employs 0.76 mm diameter fiber optic cables which are inserted transversely through the substance of the tissue and direct light onto a large silicon photo diode which tracks the point at which the light contacts the diode array. The system is synchronized so that as each fiber is illuminated in order, the diode output is sent to a multiplexer resulting in a system frequency response of approximately 3 kHz. The authors noted that hardware cost was approximately $1000. That figure did not include the circuit design, construction, testing, or calibration. The authors used this prototype device to measure tissue strains as large as 40% during a biaxial test of a flat section of the ovine right ventricle. As the fibers are transversely mounted through the section of tissue, their intrusion on the deformation was thought to be minimal. The accuracy and calibration of this method are not reported. Further, the errors due to optic fiber rotation or distortion across the cross section of the tissue that would result from a nonuniform strain field were not discussed.

Because direct contact methods using transducers are invasive, and rarely provide full-field measures of strain, noncontact methods have become increasingly more popular. These methods typically track the position of tissue markers over time to determine displacements at discrete points of the tissue and are commonly used to determine the full-field strain variation across the tissue. Obtaining tissue marker contrast and quantifying marker position are achieved using a wide variety of tools and techniques including clinical imaging systems and optical methods. Clinical imaging systems have the advantage of being able to capture images of the tissue when the region of interest cannot be directly visualized using optical methods.

Biplanar cineradiography is among the most common and oldest techniques, and has been used in a variety of applications including determining the deformations in a three-dimensional space of the beating canine heart in vivo.38,112 A number of studies have investigated the methods used for deriving the three-dimensional space from the planar images and the results of a parametric analysis of the errors associated with biplanar cineradiography have been reported.1,45,63,72,98,115 Hashima et al. used this method to track the positions of an array of 25 lead beads (1.0 mm in diameter) sewn to the epicardium of the left ventricle in an array approximately 5 to 10 mm apart.88 Frames were captured at a rate of 120 Hz but other studies report using frequencies up to 3000 Hz.37 To calibrate the system, several 1.0 cm long radiopaque rods were placed within the field and imaged. In a similar study, Waldman et al. found the error in the reconstruction of the three-dimensional displacements using biplanar cineradiography to be 0.3 mm and was limited primarily by digitization errors.112 Pin cushion distortion (warping along the edges of the image) and the cone effect (magnification dependent on distances from the focal plane) were relatively small compared to the digitizing errors (0.05 and 0.1 mm, respectively). In a later study examining errors associated with this method, Waldman and McCulloch reported that marker positions
could be located in three-dimensional space with a standard deviation of 2.5% of the full-field of view using biplane cineradiography. The recent use of magnetic resonance tagged images has eliminated the need for the invasive implantation of radiopaque markers into the tissue associated with biplanar cineradiography. The technique is based on locally perturbing the magnetization of the myocardium with selective radio-frequency saturation, resulting in multiple, thin tag planes. The imaging plane is orthogonal to the tag planes and the intersections of these planes result in dark stripes which deform with the tissue. The intersections are tracked, resulting in a spatial history of the tissue deformation. Young et al. reported using this method to track the deformations of the human heart. A total of 3100 points were tracked with an RMS error of half a pixel or 0.47 mm. An obvious advantage of the magnetic resonance tagging methods is the noninvasive ability to track the motion of an entire tissue volume including the tissue substance and the tissue surface in vivo. Current techniques, however, remain limited by the frequency and duration over which these images may be obtained and the number of institutions equipped to perform these measurements.

Optical methods have been widely used and include still photography, video, and CCD (charge coupled device) cameras. These systems track optical markers or tissue landmarks on the surface of the tissue to determine displacements. A great number of different optical markers have been used. Markers vary in size, shape, color, and material. Selection of an appropriate marker aids in tracking, improving accuracy, and minimizing the effect of the marker on strain profile. Accuracy of each of these techniques seems most tightly coupled to reliably determining an exact marker location during digitization.

Improving marker contrast to gain accuracy and ease of marker tracking has been studied extensively. Non-reflective markers can be made by blackening a surface with sulfide, ink, or paint. Fluorescent markers have also been used. Smutz et al. used fluorescent markers illuminated by an ultraviolet light source in an otherwise dark room. Others have relied on tissue-mounted LEDs. These methods have the advantage of allowing band pass filtering at the excitation frequency to improve contrast between the markers and the background.

In addition to marker contrast, the attachment of the marker to the tissue requires careful consideration. Hoffman and Grigg used stopcock grease or mineral oil to attach 600 µm disks to the posterior joint capsule of the cat knee. Other methods to attach markers are the use of histoacryl glue, cyanoacrylate glue, and small sutures. The attachment of external markers to the tissue is not without consequences. Barbee et al. validated their method of bead attachment to single smooth muscle cells by microscopically examining the substructure with and without the beads attached to insure that the cell did not reorganize with the addition of the 10 µm diameter microspheres. Investigators have also stained the tissue of interest directly with paints or ink to avoid the problems of external marker attachment. Elastin stain, Verhoeff’s stain, and India ink have all been used. While decreasing intrusion, stains typically create irregular marks with varying signal intensities whose locations may be more difficult to determine.

A majority of these methods involve placing the marker on the surface of the tissue, thus only providing data about the displacements at the surface. In an effort to measure the deformations within the substance of articular cartilage, Schinagl et al. used fluorescently stained cell nuclei as markers. Nuclei at different depths were then tracked using transmitted and epifluorescence microscopy.

In order to track the marker displacement, an image capture technique needs to be implemented. For static testing, a low method to track marker displacement is photography. The shutter time or acquisition time of a single frame must be quick enough to avoid blurring of the markers in the image. Typical video systems have a frequency response of 30 Hz, but split frame video at 60 Hz is also common. To avoid blurring of moving markers during the long exposure times of conventional video, Prinzen et al. incorporated the use of a xenon strobe which was triggered by a video frame pulse. Hoffman and Grigg described a method using a high-sensitivity television camera, a trinocular microscope, and a video image frame grabber to store the digitized image on a microcomputer for post-processing. Other investigators have recorded their images using CCD cameras that allow image acquisition rates up to and greater than 10 kHz. Microscopes can be used in conjunction with video or CCD cameras to track the positions.
of small particles.\textsuperscript{7,93} Polaroid filters have also been used to eliminate unwanted glare associated with moist tissues.\textsuperscript{85}

For three-dimensional measurements of displacement, two or more image views are obtained and reconstructed through the use of direct linear transformation methods.\textsuperscript{6,1,50,51,64,97} Sirkis and Lim described the equations used for a direct linear transform assuming a pin-hole camera, and investigated the role of possible errors in the process.\textsuperscript{97} Luo et al. examined the effects of changing the angle between the two cameras used to quantify the three-dimensional space.\textsuperscript{64} A lower limit of the pan angle was found to be 20 degrees. No improvement in accuracy was noted as pan angles increased to 40 degrees and testing at larger angles was not reported. As often occurs in biomechanical systems, planar motion data are desired from a curved or slightly irregular surface. Waldman and McCulloch and others investigated errors due to single plane vs. multiplane imaging of the curved surfaces of the heart, and provide guidelines on the maximum allowable curvature for single imager system.\textsuperscript{82,113}

Identification and tracking of markers from captured image data have received considerable attention as it can be both time intensive and error prone. Automated edge detection, grid tracking algorithms, and image correlation techniques have all been refined to improve the speed and accuracy of this time-intensive process.\textsuperscript{22,55,85,94,99,106,117} One of the first automated methods of optical strain measurement was the Video Dimension Analyzer (VDA).\textsuperscript{55,106,117} Horizontal lines stained on the tissue are captured by a video camera and displayed on a monitor with an electronic dimension analyzer which outputs a voltage based on the distance between the two lines. The frequency response of this system is approximately 20 Hz and the results are displayed in real time. The drawbacks of VDA are that only strains in one dimension are measured and the strain is averaged between the two markers. Lam et al. reported calibration of the VDA. Four different experiments were conducted to measure the accuracy of the method. First, the effect of changing camera and object distance was measured. The second and third tests measured the influence of imaging through the wall and saline environment of a test tank and the effect of changing the angle of incidence. The final test was to measure the dynamic response of the system. The accuracy of the tracking device at locating the edges of the marker lines was found to dominate the error analysis. Variations due to the above perturbations of the system did not significantly affect accuracy and overall the VDA was found to be accurate to 1\% strain.\textsuperscript{55}

Derwin et al. described an automated method to determine uniaxial strain in which horizontal stain lines spanning the cross section of the tissue are tracked through vertical displacements. To avoid discontinuities or breaks within the line, the image was smoothed by convolving the image intensity with a Gaussian function. Next, a gradient was calculated in the direction of displacement (direction must be given by the user). The gradient was then thresholded to give areas of positive and negative slope corresponding to each edge of the line. The edges were then averaged and tracked through sequential images resulting in a displacement history.\textsuperscript{22} Prinzen et al. described a method by which 43 paper markers on the surface of the heart were automatically sorted and tracked in a single plane. Strain distribution is then determined by separating the region into triangles and computing the planar strain components from the changes in the lengths of the sides of each triangle.\textsuperscript{85}

To improve marker recognition during digitization, images are often smoothed, sharpened, or enhanced. Smoothing reduces the signal intensity variation between nearby pixels, and is often used to reduce noise.\textsuperscript{49} This has the effect of eliminating pixel values that are unrepresentative of their surroundings. Median filtering is a local smoothing process in which a pixel’s intensity is replaced with the median of neighboring pixels. Since the median value must actually be the value of one of the pixels in the neighborhood, the median filter does not create unrealistic pixel values when the filter straddles an edge. For this reason the median filter is much better at preserving sharp edges than the mean filter. It is particularly useful if the characteristic to be maintained is edge sharpness.\textsuperscript{4} Image sharpening to better define the edges of the markers is often accomplished using a gradient method. The images may then be thresholded to show only marker positions against a uniform continuous background. Schinagl et al. used NIH Image 1.44 to enhance digital images obtained by CCD camera. The images were smoothed and marker edges were enhanced by convolution with a $3 \times 3$ sharpening filter and a $9 \times 9$ “Mexican Hat” filter.\textsuperscript{93}
To increase the accuracy of displacement measurements, centroid algorithms have been developed to more accurately determine marker positions.\textsuperscript{46,48,94,97,99} Centroid algorithms can improve accuracy from 0.5 pixels to as few as 0.02 pixels.\textsuperscript{96} These algorithms define the spot center as the centroid of the shaded region \((\bar{x}, \bar{y})\) given by

\[
\bar{x} = \frac{\sum\sum i \cdot (GL_{ij} - T)}{\sum\sum (GL_{ij} - T)}
\]

and

\[
\bar{y} = \frac{\sum\sum j \cdot (GL_{ij} - T)}{\sum\sum (GL_{ij} - T)}
\]

where \(GL_{ij}\) is the gray level of a pixel located at \((i, j)\) and \(T\) is a threshold level. The threshold level is chosen at a level above that of the background of the markers so that only pixels above the threshold value are used in the computation. A study by Sirkis and Lim concluded that spot sizes with a radius of about 5 pixels provided the most accurate spot position data when centroid algorithms were employed. Under optimum conditions, with centroid algorithms and lens distortion accounted for, they found that displacement measurements could be made with an accuracy of 0.015 pixels resulting in a measurement accuracy of 120 microstrains.\textsuperscript{97}

A complete calibration and sensitivity analysis of any optical system are necessary to maximize accuracy. The tools used to calibrate the space should have an accuracy one order of magnitude greater than that which is desired from the system being calibrated. A few investigators have published thorough calibration strategies for use in determining the accuracy of particular optical systems.\textsuperscript{55}

Derwin et al. reported a calibration of their single imager uniaxial strain system. Using calibration blocks, the system’s sensitivity to errors in in-plane and out-of-plane translation and rotation were measured. In addition, effects of lighting optics, shutter settings, and imaging through a glass environmental chamber with and without a circulating physiological saline bath were analyzed. Imaging through the glass and the circulating saline had no measurable effect on accuracy and accuracies between 500 and 1800 microstrains were reported.\textsuperscript{22}

Smutz et al. reported the results of a calibration experiment to determine the static and dynamic accuracy of their system (Expert Vision System, Motion Analysis Corporation, Santa Rosa, CA) and the associated effect of marker size. This system has camera speeds of 200 Hz. Static error was defined as the measured motion of the markers when they were not moving. Dynamic error was the deviation of the motion calculated by the system from the motion measured by a reference LVDT. Five marker sizes from 0.8 to 3.2 mm, five camera distances, and seven loading rates were investigated. Results of the testing were compared by normalizing parameters to the camera field of view (CFC) \((256 \times 240\) pixels). They found that static error was not a function of marker size (diameter varied from 1.6 to 50 pixels) and was equal to 0.6 pixels. Dynamic error was found to be 0.15 pixels and was independent of velocity. Consistent with the data published by Sirkis, markers with radii of 5 pixels were found to be more accurately located than smaller markers.\textsuperscript{97} For tissue gauge lengths equal to 75% of the CFV, this system can resolve infinitesimal strains with accuracy of 830 microstrains.\textsuperscript{99}

A complete calibration technique should quantify both systematic and random errors and their associated source and propagation effects. Each step of the image capture and analysis process should be evaluated. This includes the distortion effects due to tissue immersion, lens and lighting effects, image smoothing and sharpening processes, edge detection or centroid determinations, errors in the calibration of the displacement space, errors associated with fitting functions, and errors associated with differentiation to determine
strain. The entire field of view should be calibrated to determine systematic errors due to lens distortion. Errors due to specimen rotation and movement within the plane of focus, and in and out of the plane of focus should also be quantified. The final calibration technique needs to mimic as closely as possible the actual experimental protocol, including the use of identical markers, testing environment, stimulated strains, and data reduction techniques.

Uniaxial strain of annulus fibrosus fibers was measured by Stokes and Greenapple. Single fiber deformation was tracked in three dimensions using stereophotogrammetry. Two 35 mm camera images were used to determine the three-dimensional positions of the markers by using a direct linear transformation method. Seven points along the length of the fiber were tracked. A stretch ratio was calculated assuming a straight line between adjacent points referenced against a no-load condition. Errors in the technique were quantified by imposing rigid body rotations and translations on the fiber. Any measured strain was then treated as an error in the measurement technique. The digitizing procedure for a single test was conducted seven times to measure the repeatability of the digitizing process. The standard deviation in determining the point positions was found to be 0.05 mm resulting in a repeatability error in strain measurement of less than 1%.

Measurement of the complete strain tensor is often achieved by examining three points placed in close proximity. For example, the Lagrangian strains on the surface of a tissue may be derived using the relation.

$$ds^2 - dS^2 = 2E_{ij}da^idaj$$ \quad i, j = 1, 2 \quad (5.20)$$

where $ds^2$ is the deformed length, $dS^2$ is the undeformed length, and $da^i$ is the change in length in the direction $i$. Letting $P'_i$ and $P_i$ denote the initial and final positions of three points undergoing a general planar deformation, as shown in Figure 5.3, the change in length of side $a$ in the $x$-direction, $\delta a_x$, is given by

$$\delta a_x = (P'_{3x} - P_{1x}) - (P'_{3x} - P'_{1x})$$ \quad (5.21)$$

and in the change in length in the $y$-direction, $\delta a_y$, is given by

$$\delta a_y = (P'_{3y} - P_{1y}) - (P'_{3y} - P'_{1y})$$ \quad (5.22)$$

The initial length of the side $a$, $L_a$, is given by

$$L'_a = (P'_{3x} - P'_{1x})^2 + (P'_{3y} - P'_{1y})^2)^{1/2}$$ \quad (5.23)$$
and the deformed length of side \( a \) is given by

\[
L_a = \left( (P_{3X} - P_{1X})^2 + (P_{3Y} - P_{1Y})^2 \right)^{1/2}
\]  

(5.24)

Applying Eq. 5.18 directly for side \( a \), we obtain

\[
L_a^2 - L_a'^2 = 2E_{xx}(\delta a_x)^2 + 4E_{xy}\delta a_x\delta a_y + 2E_{yy}(\delta a_y)^2
\]  

(5.25)

Using this approach for sides \( b \) and \( c \) results in three equations and the unknowns; \( E_{xx}, E_{xy} \) and \( E_{yy} \), can be solved for directly. Principal strains can be calculated solving the eigenvalue problem.

With tissue property and geometry variations, uniform loads give rise to nonhomogenous strain fields. As a result, it often becomes necessary to determine the full-field strain distribution across the region of interest in the tissue. Zerniche et al. found regional surface strains near the clamp during tendon testing to be twice the value of strains in the middle of the test specimen. Further, tissue heterogeneity and the presence of an active component in muscle imply, when measuring isometric strains in a muscle tendon unit, that the strain within the structure may be changing. Van Bavel et al. simultaneously measured the strains in both the aponeurosis and muscle belly of the rat medial gastrocnemius by tracking at least three markers’ displacements in the region and by directly computing the Green-Lagrange strains. Trestic and Lieber reported that this relative shortening of passive structures and shortening within the muscle belly resulted in 20% differences in predicted muscle force in the frog gastrocnemium. Without regional measurements of tendon, aponeurosis, and muscle strains in their experiment, these effects might go unnoticed.

In an effort to improve accuracy and reduce noise in full-field strain measurement, investigators have fitted the surface displacement across the entire tissue surface with a function and then differentiated the function to attain the strain at each point. Sutten et al. described a method which optimized smoothing parameters to remove Gaussian noise on two-dimensional displacement data. Best et al. fit displacement data with a function to determine one-dimensional uniaxial finite strain in the rabbit tibialis anterior. Approximately 50 marks were stained along the muscle from origin to insertion (Fig. 5.4). Image data were collected on a 1000 Hz, 238 × 192 pixel CCD camera. Axial deformation, \( u \), vs. initial position of the marker on the tissue, \( x \), was digitized for each image, resulting in a complete \( u(x) \) history (Fig. 5.5). Strain was calculated using the Lagrangian formulation (Eq. 5.15). While tensile axial deformations of the muscle were large, transverse deformations and the change in transverse deformation with respect to the initial position, \( x \), were small. At maximum displacement, \( dv/dx \) was less than 0.06; therefore, \( (dv/dx)^2 \) was less than 0.0036. Similarly, \( (dw/dx)^2 \) was less than 0.0009 at maximum displacement. Therefore, the Eq. 5.15 was simplified to

\[
E_{ss}(x, t) = \frac{\partial u(t)}{\partial x} + \frac{1}{2} \left( \frac{\partial u(t)}{\partial x} \right)^2
\]  

(5.26)

To illustrate the advantages obtained by fitting a continuous function to the displacement, derivatives of the axial displacement, \( u(x) \), were determined by either a central difference method on the raw data or by differentiation of a third or fourth order polynomial fit of the displacement data (Fig. 5.6). With this particular model, the structure had a gauge length of 6 cm, and failed when elongated to 9 cm. Given the limited spatial resolution of the imager, this resulted in a position resolution of approximately 0.5 mm/pixel. Strains calculated using a central difference method from the noisy, discretized data produced errors on the order of the strain amplitude. Recognizing that discretization error is randomly distributed, fitting a function to a set of points decreases error by \( 1/\sqrt{n} \) where \( n \) is the number of points in the fitted curve. In these experiments, this resulted in a decrease in error by a factor of 6.3. While splines tended to have oscillations that produced negative strains when differentiated, polynomial functions were well-behaved and were insensitive to the order of the polynomial (Fig. 5.6).
When fitting functions to multiple marker positions, a tradeoff between marker size and the number of markers occurs. While both reduce error, increasing marker size decreases the number of marks which can be placed on the surface. As the purpose of this technique is to minimize the error in the strain field and not the position of each spot, it becomes necessary to optimize the benefits of larger spot size with the benefits of greater numbers of spots. To that end, we generated numerical strain fields from previously performed experiments to assess the effect of spot radii and number of spots on strain measurement.

**FIGURE 5.4** Digital image of the rabbit tibialis anterior with three sets of surface spots. The muscle origin is to the right. The distal tendon, left, is inserted into the grip of a hydraulic actuator. Deflections in both the lateral and axial directions were quantified by digitizing the black surface marks.

**FIGURE 5.5** Discretized displacement of the surface markers on the rabbit tibialis anterior during passive elongation. These data illustrate the decrease in quantization error associated by fitting the displacement field with a polynomial function.
accuracy. To determine the optimal spot size, a series of simulations was performed to emulate the CCD camera’s data acquisition. Specifically, an algorithm was developed which placed a spot of a given radius at a random location over the pixel array. Each pixel was then assigned a gray level from 0 to 255. Based on a sample of 40 spots collected using this imaging system, the pixels completely covered by a spot were assigned a gray level of 229 ± 9.6, and the pixels that were completely uncovered were assigned a background gray level of 171 ± 6.0. Addition of the variation in pixel signal was found to profoundly influence the results, illustrating the dependence of accuracy on the unique features of the particular system under study. It also illustrates the need to calibrate and optimize each new experiment and test system.

For those pixels partially covered by a spot, a Monte Carlo routine was developed to determine the area fractions of spot and background. Gray level, $GL$, was then calculated based on the area fraction occupied by the spot, $f$, the spot’s gray level, $GL_s$, the area fraction occupied by the background, $1 – f$, and the background gray level, $GL_b$, using the following equation:

$$GL = f \cdot GL_s + (1 – f) \cdot GL_b \tag{5.27}$$

Defining accuracy as the RMS error in surface strain along the length of the muscle, the effects of spot number vs. spot size were determined. Using this technique, we found that RMS strain error was minimized over a range of spot radii from approximately 2 to 7 pixels (Fig. 5.7). Because of spot distortions that occur in large spots in nonuniform strain fields, we suggest that the spot size chosen be toward the smaller end of this range.
Finite element analysis (FEA) has also been employed to determine nonhomogenous strain fields. Markers placed on the surface of the specimen serve as nodes for the finite elements. The complete strain tensor can then be calculated at the Gauss points of the element. In addition, using interpolation functions, strain distribution throughout the element can be calculated. Specific marker placements need not be colinear nor regularly placed, and marker density can be increased in areas of high strain variation. Finite element methods may be used in both planar and three-dimensional analyses. Hoffman and Grigg used this method to determine strains within the posterior joint capsule of the cat knee using planar linear elements. Hashima et al. used a least squares method and bicubic Hermite isoparametric elements to fit successive three-dimensional marker positions of the surface of a beating canine heart. Sutton et al. described a penalty method used in conjunction with FEA techniques to fit noisy displacement data and determine strains. Waldman and McCulloch investigated the effect of random errors introduced by Gaussian noise on the calculated strain field, finding that the FEA method reduced the errors in the strain field introduced by Gaussian noise by 50%.

**5.5 Conclusion**

Analysis of strain in muscle has evolved considerably. Beginning with average stretches measured by simple transduction of actuator motion, to more complex and expensive optical measurement systems, and progressing to full-field, three-dimensional large strain tensorial measurement systems based on magnetic resonance and finite element techniques, the choices available to the investigator are vast. Regardless of available resources, this review demonstrates the importance of proper definition of the strain quantities to be determined and the importance of controlling the physiologic environment in which the tissue deformation is measured. It also illustrates the need to carefully design the measurement and data reduction strategy to quantify and minimize error. This is particularly true of optical systems.
in which contrast, variation in contrast, spot size, and other variables all influence system accuracy, and the selection of the optimal system can only be achieved following careful experimental evaluation.

References


